A nonrandom dynamic component in the synaptic noise of a central neuron

(chaos/recurrence plot/unstable periodic orbit/auditory inputs/attention)

PHILIPPE FAURE AND HENRI KORN

Biologie Cellulaire et Moléculaire du Neurone, Institut National de la Santé et de la Recherche Médicale U-261, Institut Pasteur, 25 Rue du Docteur Roux, 75724 Paris Cedex 15, France

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ABSTRACT Continuous segments of synaptic noise were recorded in vivo from teleost Mauthner cells and were studied with the methods of nonlinear analysis. As in many central neurons, this ongoing activity is dominated by consecutive inhibitory postsynaptic potentials. Recurrence plots and first or second order Poincaré maps combined with surrogate shuffling revealed nonrandom patterns consistent with the notion that synaptic noise is a continuously varying mixture of periodic and chaotic phases. Chaos was further demonstrated by the occurrence of unstable periodic orbits. The nonrandom component of the noise is reproducibly and persistently reduced when the level of background sound, a natural stimulus for networks afferent to the Mauthner cell, is briefly elevated. These data are consistent with a model involving a reciprocally connected inhibitory network, presynaptic to the Mauthner cell and its intrinsic properties. The presence of chaos in the inhibitory synaptic noise that regulates the excitability of the Mauthner cell and its sensitivity to external stimuli suggests that it modulates this neuron’s function, namely to trigger a fast escape motor reaction following unexpected sensory information.

The membrane potential of vertebrate central neurons fluctuates constantly. Although this process, called synaptic noise, is ubiquitous, its fine structure is poorly documented. Synaptic noise is due to the postsynaptic actions of packets of neurotransmitters, or quanta, released from afferent synapses as a consequence of intermittent firing of the parent neurons. It has been suggested that these summed fluctuations reflect the firing pattern of presynaptic networks, that they modulate the input/output relations of neurons (1–3), and that they are necessary for the implementation of some theoretical neuronal networks (4, 5).

Synaptic noise has been commonly considered to be stochastic (2, 6, 7) and is often modelled as such (8, 9). However, it is now possible to generate a refined description of its structure with nonlinear dynamic analysis, which has been particularly useful in various fields in which apparently random phenomena have hidden specific structures that cannot be resolved with linear tools (10). The question of the presence of nonlinear dynamics in the brain (11–13), and particularly of chaos, arises naturally in view of its properties (sensitivity to initial conditions and ability to switch among many different modes), which also characterize biological behaviors (13).

Despite the severe limitations in identifying chaos due to the possible mixture of different dynamics (14), we have applied this methodology to study the temporal structure of synaptic noise recorded in vivo from a central neuron, namely the Mauthner cell (M-cell) of teleosts. We show features of chaos in this signal.

Synaptic Noise in the M-Cell

Spontaneous activity was recorded with KCl-filled microelectrodes in the proximal part of the M-cell lateral dendrite of adult goldfish (Carassius auratus, n = 5) and zebrafish (Brachydanio rerio, n = 5) with similar results for both. Animals were anaesthetized with 3-aminobenzoic ethyl ester acid (MS 222; Sandoz Pharmaceutical), immobilized with Flaxedil (Rhône-Poulenc) or pancuronium bromide, and continuously perfused with water. As shown in Fig. 1A, this activity is generated by two groups of glycinergic interneurons, one of which can be driven by auditory inputs (15) and it consists, mainly (1), of consecutive inhibitory postsynaptic potentials (IPSPs). With Fourier analysis, most spectra were dominated by a noisy broadband background, which could reflect either a stochastic process or chaos (10). Thus, more sophisticated tools were required to identify deterministic structures (such as periodic and/or chaotic ones) that could otherwise be considered as stochastic. For this purpose, synaptic noise was first digitized at 24 kHz for visual inspection. To achieve a compromise between computation time and sampling rate, the latter was taken as 1.5 or 3 kHz for RPs and 3 kHz for Poincaré maps. As shown in Fig. 1A (Right) this rate was sufficient for representing the whole signal, including its fast rising time to peak and for studies of correlations between closely spaced IPSPs. The analysis was done with homemade programs written in Labview 4 for Macintosh Power Computers.

Evidence in RPs for Nonrandom Components of Synaptic Noise

We first used RP analysis to locate recurring patterns and to reveal dynamic behaviors possibly hidden in the biological signal (16). For RPs, minimal size or stationarity, which are not often observed in biological systems, are not necessary. RPs portray the dynamics of the embedded signals in the form of distinctive patterns of dots interspersed in a square matrix. Plots were constructed (Appendix A) with a d-dimensional signal using the method of time delays applied on 2-sec epochs of activity (Fig. 1 B1 and C1). These plots already suggested the existence of nonrandom motions. For example, they showed dot organizations resembling chaos (Fig. 1 B1 and B2) or a periodical activity, regular or intermittent, ranging from 20 to 80 Hz superimposed with aperiodic figures, also compatible with nonlinear dynamics (Fig. 1 C1 and C2). A significant variability of these patterns was apparent not only among different preparations but also during the same experiment (data not shown). In contrast, homogenous fillings indicative

Abbreviations: M-cell, Mauthner cell; IPSP, inhibitory postsynaptic potential; VIII n., eighth nerve; RP, recurrence plot; PM, Poincaré map; UPO, unstable periodic orbit.
of a stochastic process, as exemplified in Fig. 1D, were never observed in our RPs.

Two parameters were available to validate the conclusions obtained with the visual inspection of the RPs (17). The first, called ratio (R), is the number of dots included in upward diagonal line segments, divided by the total number of points; it quantifies the degree to which the signal is deterministic. The second, or entropy (E), describes the distribution of the lengths...
of the different line segments. Both terms are temporal sequence-sensitive (Appendix A). They were used to assess the statistical significance of the RPs with the help of surrogates (Appendix B), i.e., of randomized representations of the original data files according to random, Gaussian scaled (18), and Fourier shuffle (19) algorithms. In this experimental series, $R$ and $E$ were calculated on RPs obtained from series of nonoverlapping 1-sec successive segments with the same cutoff, $r$, in each experiment, a lag of 33 msec (first minimum of the autocorrelation function), an embedding dimension of 5, and a sampling frequency $F_s = 1.5$ kHz, and they were compared with those obtained with $n = 100$ Fourier shuffle surrogates. The null hypothesis was rejected in 239/275 successive 1-sec windows, extracted from the four experiments that were tested.

**Different Patterns of Noise Identified with Poincaré Maps (PMs)**

Several converging approaches are necessary to identify nonlinear patterns and avoid spurious identification of chaos. Also, RPs treat signals as a whole, including instrumental noise. Thus we converted the signals into sequences of events $(I_n, I_{n+1})$ to obtain PMs of interevent intervals (20). These events were extracted from the raw data (Fig. 2A Left) using the time derivative of the individual synaptic potentials (Fig. 2A Right), a procedure that allows the detection of IPSPs even when they overlap. As the threshold $T$ used for constructing maps was lowered, the number of detected events increased, and several typical patterns emerged, indicating that synaptic noise can combine several dynamics. For example, PMs changed from periodic, with constant intervals between points, indicating a frequency of 35 Hz (Fig. 2B1, $T_1$), to high dimensional, i.e., without evidence of a typical structure (Fig. 2B1, $T_3$). The transition between these extremes was marked by a triangular motif, due presumably to the random occurrence of at most one event between each period (Fig. 2B1, $T_2$). Chaotic patterns characterized by extended structures that are not sets of points could also be present at high thresholds (Fig. 2B2, $T_1$), and they were progressively blurred at lower values

![Fig. 2. Mixtures of dynamic behaviors revealed by first order PMs. (A) Sampled (3-kHz) synaptic noise (Left) and its first derivative (Right), illustrating the threshold method; events detected above a given level (labeled $T_1$, $T_2$, and $T_3$) were used to plot the $n$th interval against the previous one. (B1 and B2) Resulting maps obtained from 30 sec of continuous recordings, in two different experiments. (B1) From the same data set as that partially shown in A. As the threshold is lowered, the pattern initially periodic (Left, $T_1$) becomes triangular (Center, $T_2$). (B2) The return maps show series of points which are not space filling and suggest chaos (Left) or attracting clusters centered around a period of 25 msec (Center). Note that in both experiments, the return maps are high dimensional for the lowest values of $T$ ($T_3$, Right).](image-url)
of $T$ (Fig. 2B, $T_2$ and $T_3$). Finally, high dimensional organizations could dominate in the return maps (not shown).

In retrospect, it was noted that the most effective thresholds for distinguishing these contrasting patterns were those which isolated the largest IPSPs, including composite ones (for $T_1$ and $T_2$) or which included all signals, except most monoquantal IPSPs and small excitatory events propagated from the distal dendrite (for $T_3$).

Confirmation of Chaotic Patterns with Unstable Periodic Orbits (UPOs)

We searched for UPOs (20–23), as an alternative to conventional measures of chaos that yield equivocal results in living tissues (20, 23, 24). UPOs found in PMs (Fig. 3A and B) consist of sequences of points approaching a fixed one on the identity line with ever-decreasing separations, followed by a sequence of points departing at ever-increasing distances (22). Evidence that they obey the specific rules of unstable fixed point behavior (20, 22, 23) is illustrated in Fig. 3C. The occurrence of UPOs (>1 per 100 events) was more common in low threshold maps. Their significance was tested with Fourier shuffle surrogates (Appendix B) constructed for each threshold series ($n = 500$), with values of $K \approx 2.5$ in six out nine fish tested.

Sudden Sounds Modify Chaotic Patterns

To test whether this dynamic system is sensitive to environmental changes, we investigated the effects of sensory stimuli known to reach the M-cell. In all trials, sounds (100 msec, 500 Hz, 75–90 dB) initiated bursts of excitatory synaptic events which, as expected (25) were in phase with the acoustic signal and were at twice its frequency (data not shown). These were accompanied by transient changes in the composition of the inhibitory synaptic noise (Fig. 4A) consisting of an initial increase followed by a longer lasting decrease in $R$ (Fig. 4B1–B3), a result found in 17 of 21 trials, in the four fish that were tested. This persistent decrease was due to changes in noise pattern rather than in amplitude distribution, as confirmed by the stability of $R$ derived from surrogates (Fig. 4C) having the same mean and variance as the original data (P. Rapp, personal communication). While a reduction in this parameter indicates a corresponding decrement of the nonrandom component, it does not allow one to distinguish the relative shifts of the periodic and chaotic signals. Regardless, its modifications persisted for at least 60 sec (Fig. 4D), even though visually, synaptic noise had apparently returned to its control state earlier.

Discussion

Taken together, our results suggest that the spike-evoked components of synaptic noise are “deterministic” and controlled by sensory inputs. Specifically, the revealed nonrandom patterns represent nonstationary mixtures of periodic and chaotic phases. These features are typical of biological systems that do not allow the use of correlation dimensions and Lyapunov exponents to further quantify chaos (10, 17, 27).

It is remarkable that inhibitory processes exhibit chaotic properties in vivo, including a deterministic control by natural stimuli, such as sound. The origin of this nonlinear dynamic is unclear, but its most likely explanations must take into consideration the organization of the networks that generate synaptic noise in the M-cell. Fig. 1A shows that primary auditory fibers activate the commissural interneurons on each side of the brain. The question then becomes whether a reciprocal inhibitory circuit can undergo a sustained activity, which is required for generating complex dynamics (28, 29). We designed a numerical model (unpublished work) incorpo-
rating the VIII n. activated connections (outlined in Fig. 1A), with internal self-sustained excitatory reentries generated by the postanodal excitations that always follow hyperpolarizations in M-cell presynaptic interneurons (30). External drives of the system were “spike activities” in the VIII n., designed to include both stochastic and periodic discharges as demonstrated experimentally (25, 31). This model showed that once activated, the presynaptic networks produce most patterns found in this study. As also noted elsewhere (32), “chaos” is not observed when the postanodal rebounds are omitted. Conversely, it is more conspicuous if large hyperpolarizations generate bursts of action potentials rather than single spikes (Fig. 1A Inset). It remains to be determined if additional network features are necessary to account for dynamic modifications of R. For example, if other excitatory drives to the inhibitory interneurons (Fig. 1A) or learning properties of inhibitory synapses (33) have a significant role.

In vivo studies should reveal comparable situations in higher vertebrate structures, such as hippocampus, cerebellum, and cortex (34), where synaptic noise is intense, and also predominantly inhibitory, and neural connections include rhythmically firing cells and oscillators.

It is difficult to envision the role of nonlinear dynamics at the cellular level, but it is known that chaotic systems can be controlled by external perturbations. Relevant here is that inhibition guarantees that the M-cell-mediated escape reaction is triggered by appropriate stimuli (15). Thus, inhibitory noise is part of a process that, similar to that underlying attention in higher vertebrates, filters improper information (35). Accordingly, the M-cell’s adaptive motor function could be eased by the stabilizing properties of UPOs (20, 22, 36), chaos also favoring state transitions initiated by varying sensory cues (29).

Appendix A: RPs

Let X(i) be the ith point on an orbit describing the system in a d-dimensional space. Then RPs are N × N arrays, in which a dot is placed at (i, j) whenever X(i) is close to X(j). Given a voltage...
the d-dimensional signal $X(i)$ can be obtained using the time delays method $X(i) = (V_i, V_{i+L}, \ldots, V_{i+(d-1)L})$, where $d$ and $L$ are the embedding dimension and the lag, respectively. Each matrix contains $N_s^2$ points, where $N_s$ is the number of vectors. For this study, $L$ was chosen as the first minimum of the average mutual information function or of the autocorrelation function. A dot was plotted at each point $(i, j)$ whenever $X(i)$ and $X(j)$ were located within a given radius, $r$. If $N_j$ is the number of vectors near $X(j)$, there are $\sum_{i=1}^{N_j} N_j^2$ dots in the RP. In this work, $r$ was fixed (constant volume construction) and determined so that $\sum_{i=1}^{N_j} N_j^2 = k$, to allow comparisons between successive plots. The ratio $(R)$ and entropy ($E$) were calculated on RPs using windows of 1 sec. This short duration guarantees a success of the method is known as that of the surrogate strategy (18). The ratio $(R)$ and entropy ($E$) were calculated on RPs using windows of 1 sec. This short duration guarantees a success of the mean and standard deviation, respectively, of these number of UPOs) was assessed using method is known as that of the surrogate strategy (18).

Appendix B: Surrogates

With a finite time series of noisy data, the problem of detecting nonlinearity is a matter of statistical measure. Several randomization representations of the original data can be used. This method is known as that of the surrogate technique (18). The statistical significance of the derived values (ratio, entropy, and number of UPOs) was assessed using $K = (N - \langle N_i \rangle)/\sigma$, where $N$ is the value of the measure in the original series, and $\langle N_i \rangle$ and $\sigma$ are the mean and standard deviation, respectively, of these parameters in surrogates. Assuming Gaussian statistics, the probability $P_s$ that $N_s \leq N$ is given by $P_s = P(N_s \leq N) = (1 + erf(\sigma/\sqrt{2}))$. A limit of $K = 2.5$ indicates a confidence level of $>99.4\%$.

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